

GATE - 2005

ME : Mechanical Engineering

Duration : Three Hours

Maximum Marks : 150

Read the following instructions carefully.

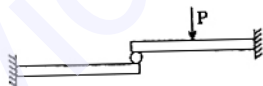
1. This question paper contains all objective questions. Q. 1 to Q. 30 carry one mark each and Q. 31 to Q. 80 carry two marks each. Q. 81 to Q. 85 each contains part "a" and "b". In these questions, parts "a" as well as "b" carry two marks each.
2. Answer all the questions.
3. Questions must be answered on special machine gradable Objective Response Sheet (ORS) by darkening the appropriate bubble (marked A, B, C, D) against the question number on the left hand side of the ORS, using HB pencil. Each question has only one correct answer. In case you wish to change an answer, erase the old answer completely using a good soft eraser.
4. There will be **NEGATIVE** marking. In Q.1 to Q. 30, 0.25 mark will be deducted for each wrong answer and in Q. 31 to Q. 80, 0.5 mark will be deducted for each wrong answer. In Q. 81 to Q. 85, for the part "a", 0.5 mark will be deducted for a wrong answer. Marks for correct answers to part "b" of Q. 81 to Q. 85 will be given only if the answer to the corresponding part "a" is correct. However, there is no negative marking for part "b" of Q. 81 to Q. 85. More than one answer bubbled against a question will be deemed as an incorrect response.
5. Write your registration number, name and name of the centre at the specified locations on the right half of the ORS.
6. Using HB pencil, darken the appropriate bubble under each digit of your registration number and the letters corresponding to your paper code.
7. Calculator is allowed in the examination hall.
8. Charts, graph sheets or tables are not allowed.
9. Use the blank pages given at the end of the question paper for rough work.
10. This question paper contains 24 printed pages including pages for rough work. Please check all pages and report, if there is any discrepancy.

Q.1–Q. 30 carry one mark each

- Stokes theorem connects
 - a line integral and a surface integral
 - a surface integral and a volume integral
 - a line integral and a volume integral
 - gradient of a function and its surface integral
- A lot has 10% defective items. Ten items are chosen randomly from this lot. The probability that exactly 2 of the chosen items are defective is
 - 0.0036
 - 0.1937
 - 0.2234
 - 0.3874
- $\int_{-a}^a (\sin^6 x + \sin^7 x) dx$ is equal to
 - $2 \int_0^a \sin^6 x dx$
 - $2 \int_0^a \sin^7 x dx$
 - $2 \int_0^a (\sin^6 x + \sin^7 x) dx$
 - zero
- A is a 3×4 real matrix and $Ax = b$ is an inconsistent system of equations. The highest possible rank of A is
 - 1
 - 2
 - 3
 - 4
- Changing the order of the integration in the double integral leads to $I = \int_{x/4}^8 \int_0^2 f(x, y) dy dx$ leads to

$$I = \int_r^s \int_p^q f(x, y) dy dx$$
. What is q ?
 - 4y
 - $16y^2$
 - x
 - 8
- The time variation of the position of a particle in rectilinear motion is given by $x = 2t^3 + t^2 + 2t$. If v is the velocity and a the acceleration of the particle in consistent units, the motion started with
 - $v = 0, a = 0$
 - $v = 0, a = 2$
 - $v = 2, a = 0$
 - $v = 2, a = 2$

- A simple pendulum of length 5 m, with a bob of mass 1 kg, is in simple harmonic motion. as it passes through its mean position, the bob has a speed of 5 m/s. The net force on the bob at the mean position is
 - zero
 - 2.5 N
 - 5 N
 - 25 N
- A uniform, slender cylindrical rod is made of a homogeneous and isotropic material. The rod rests on a frictionless surface. The rod is heated uniformly. If the radial and longitudinal thermal stresses are represented by σ_r and σ_z , respectively, then
 - $\sigma_r = 0, \sigma_z = 0$
 - $\sigma_r \neq 0, \sigma_z = 0$
 - $\sigma_r = 0, \sigma_z \neq 0$
 - $\sigma_r \neq 0, \sigma_z \neq 0$
- Two identical cantilever beams are supported as shown, with their free ends in contact through a rigid roller. After the load P is applied, the free ends will have
 - equal deflections but not equal slopes
 - equal slopes but not equal deflections
 - equal slopes as well as equal deflections
 - neither equal slopes nor equal deflections



- equal deflections but not equal slopes
 - equal slopes but not equal deflections
 - equal slopes as well as equal deflections
 - neither equal slopes nor equal deflections
- The number degrees of freedom of a planar linkage with 8 links and 9 simple revolute joints is
 - 1
 - 2
 - 3
 - 4
 - There are four samples P, Q, R and S, with natural frequencies 64, 96, 128 and 256 Hz, respectively. They are mounted on test setups for conducting vibration experiments. If a loud pure note of frequency 144 Hz is produced by some instrument, which of the samples will show the most perceptible induced vibration?
 - P
 - Q
 - R
 - S
 - Which one of the following is a criterion in the design of hydrodynamic journal bearings?
 - Sommerfeld number
 - rating life
 - Specific dynamic capacity
 - Rotation factor

13. The velocity components in the x and y directions of a two dimensional potential flow are u and v , respectively. Then $\frac{\partial u}{\partial x}$ is equal to

(a) $\frac{\partial v}{\partial x}$ (b) $-\frac{\partial v}{\partial x}$
(c) $\frac{\partial v}{\partial y}$ (d) $-\frac{\partial v}{\partial y}$

14. In a case of one dimensional heat conduction in a medium with constant properties, T is the temperature at position x , at time t . Then $\frac{\partial T}{\partial t}$ is proportional to

(a) $\frac{T}{x}$ (b) $\frac{\partial T}{\partial x}$
(c) $\frac{\partial^2 T}{\partial x \partial t}$ (d) $\frac{\partial^2 T}{\partial x^2}$

15. The following four figures have been drawn to represent a fictitious thermodynamic cycle, on the $p-v$ and $T-s$ planes.

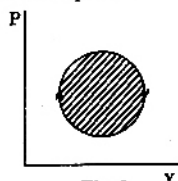


Fig. 1

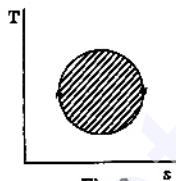


Fig. 2

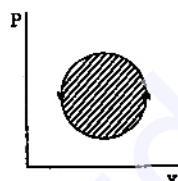


Fig. 3

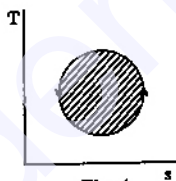
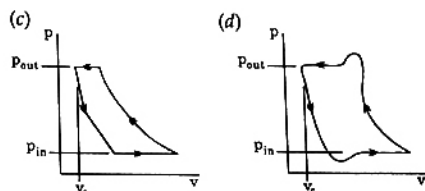
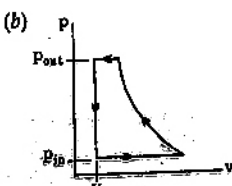
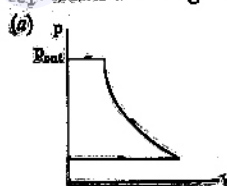


Fig. 4

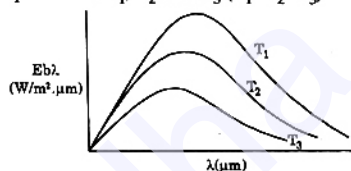
According to the first law of thermodynamics, equal areas are enclosed by

- (a) figures 1 and 2 (b) figures 1 and 3
(c) figures 1 and 4 (d) figures 2 and 3

16. A $p-v$ diagram has been obtained from a test on a reciprocating compressor. Which of the following represents that diagram?



17. The following figure was generated from experimental data relating spectral black body emissive power to wavelength at three temperatures T_1 , T_2 and T_3 ($T_1 > T_2 > T_3$).



The conclusion is that the measurements are

- (a) correct because the maxima in $E_{b\lambda}$ show the correct trend
(b) correct because Planck's law is satisfied
(c) wrong because the Stefan Boltzmann law is not satisfied
(d) wrong because Wien's displacement law is not satisfied

18. For a typical sample of ambient air (at 35°C , 75% relative humidity and standard atmospheric pressure), the amount of moisture in kg per kg of dry air will be approximately

- (a) 0.002 (b) 0.027
(c) 0.25 (d) 0.75

19. Water at 42°C is sprayed into a stream of air at atmospheric pressure, dry bulb temperature of 40°C and a wet bulb temperature of 20°C . The air leaving the spray humidifier is not saturated. Which of the following statements is true?

- (a) Air gets cooled and humidified
(b) air gets heated and humidified
(c) Air gets heated and dehumidified
(d) Air gets cooled and dehumidified

20. Match the items of List I (Equipment) with the items of List II (Process) and select the correct answer using the given codes.

List I (Equipment)	List II (Process)
P - Hot Chamber Machine	1. Cleaning
Q - Muller	2. Core making
R - Dielectric Baker	3. Die casting
S - Sand Blaster	4. Annealing
	5. Sand mixing

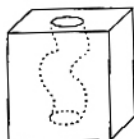
- (a) P-2, Q-1, R-4, S-5 (b) P-4, Q-2, R-3, S-5
(c) P-4, Q-5, R-1, S-2 (d) P-3, Q-5, R-2, S-1

21. When the temperature of a solid metal increases,
- strength of the metal decreases but ductility increases
 - both strength and ductility of the metal decrease
 - both strength and ductility of the metal increase
 - strength of the metal increases but ductility decreases

22. The strength of a brazed joint
- decreases with increase in gap between the two joining surfaces
 - increases with increase in gap between the two joining surfaces
 - decreases up to certain gap between the two joining surfaces beyond which it increases
 - increases up to certain gap between the two joining surfaces beyond which it decreases

23. A zigzag cavity in a block of high strength alloy is to be finish machined. This can be carried out by using

- electric discharge machining
- electro-chemical machining
- laser beam machining
- abrasive flow machining

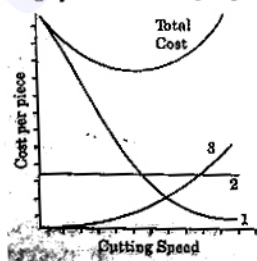


24. In order to have interference fit, it is essential that the lower limit of the shaft should be
- greater than the upper limit of the hole
 - lesser than the upper limit of the hole
 - greater than the lower limit of the hole
 - lesser than the lower limit of the hole

25. When 3-2-1 principle is used to support and locate a three dimensional work-piece during machining, the number of degrees of freedom that are restricted is

- 7
- 8
- 9
- 10

26. The figure below shows a graph which qualitatively relates cutting speed and cost per piece produced.



The three curves 1, 2 and 3 respectively represent

- machining cost, non-productive cost, tool changing cost
- non-productive cost, machining cost, tool changing cost
- tool changing cost, machining cost, non-productive cost
- tool changing cost, non-productive cost, machining cost

27. Which among the NC operations given below are continuous path operations?

Arc Welding (AW)	Milling (M)
Drilling (D)	Punching is Sheet Metal (P)
Laser Cutting of Sheet Metal (LC)	Spot Welding (SW)

- AW, LC and M
- AW, D, LC and M
- D, LC, P and SW
- D, LC, and SW

28. An assembly activity is represented on an Operation Process Chart by the symbol

- AA
- A
- D
- O

29. The sales of a product during the last four years were 860, 880, 870 and 890 units. The forecast for the fourth year was 876 units. If the forecast for the fifth year, using simple exponential smoothing, is equal to the forecast using a three period moving average, the value of the exponential smoothing constant α is

- $\frac{1}{7}$
- $\frac{1}{5}$
- $\frac{2}{7}$
- $\frac{2}{5}$

30. Consider a single server queuing model with Poisson arrivals ($\lambda = 4/\text{hour}$) and exponential service ($\mu = 4/\text{hour}$). The number in the system is restricted to a maximum of 10. The probability that a person who comes in leaves without joining the queue is

- $\frac{1}{11}$
- $\frac{1}{10}$
- $\frac{1}{9}$
- $\frac{1}{2}$

Q. 31 to Q. 80 carry two marks each.

31. Which one of the following is an eigenvector of the

matrix $\begin{bmatrix} 5 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 \\ 0 & 0 & 2 & 1 \\ 0 & 0 & 3 & 1 \end{bmatrix}$?

(a) $\begin{bmatrix} 1 \\ -2 \\ 0 \\ 0 \end{bmatrix}$

(b) $\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$

(c) $\begin{bmatrix} 1 \\ 0 \\ 0 \\ -2 \end{bmatrix}$

(d) $\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$

32. With a 1 unit change in b , what is the change in x in the solution of the system of equations $x + y = 2$, $1.01x + 0.99y = b$?

- (a) zero (b) 2 units
(c) 50 units (d) 100 units

33. By a change of variables $x(u, v) = uv$, $y(u, v) = v/u$ in a double integral, the integrand $f(x, y)$ changes to $f(uv, u/v) \phi(u, v)$. Then, $\phi(u, v)$ is

- (a) $\frac{2v}{u}$ (b) $2uv$
(c) v^2 (d) 1

34. The right circular cone of largest volume that can be enclosed by a sphere of 1 m radius has a height of

- (a) $\frac{1}{3}$ m (b) $\frac{2}{3}$ m
(c) $\frac{2\sqrt{2}}{3}$ m (d) $\frac{4}{3}$ m

35. If $x^2 \frac{dy}{dx} + 2xy = \frac{2 \ln x}{x}$, and $y(1) = 0$, then what is

- (a) $\frac{1}{e}$ (b) 1
(c) $\frac{1}{e^2}$ (d) $\frac{1}{e^2}$

36. The line integral $\int \vec{V} \cdot d\vec{r}$ of the vector function

$\vec{V} = 2xyz\hat{i} + x^2z\hat{j} + k^2y\hat{k}$ from the origin to the point $(1, 1, 1)$

- (a) $\frac{1}{2}$ (b) $\frac{1}{2}$
(c) $\frac{1}{2}$ (d) $\frac{1}{2}$

37. Starting from $x_0 = 1$, one step of Newton-Raphson method in solving the equation $x^3 + 3x - 7 = 0$ gives the next value (x_1) as

- (a) $x_1 = 0.5$ (b) $x_1 = 1.406$
(c) $x_1 = 1.5$ (d) $x_1 = 2$

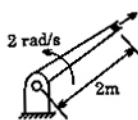
38. A single die is thrown twice. What is the probability that the sum is neither 8 nor 9?

- (a) $\frac{1}{9}$ (b) $\frac{5}{36}$
(c) $\frac{1}{4}$ (d) $\frac{3}{4}$

39. Two books of mass 1 kg each are kept on a table, one over the other. The coefficient of friction on every pair of contacting surfaces is 0.3. The lower book is pulled with a horizontal force F . The minimum value of F for which slip occurs between the two books is

- (a) zero (b) 1.06 N
(c) 5.74 N (d) 8.83 N

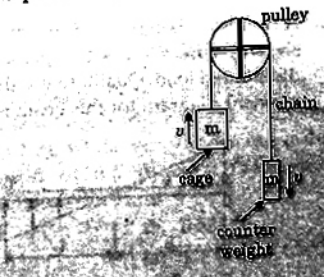
40. A shell is fired from a cannon. At the instant the shell is just about to leave the barrel, its velocity relative to the barrel is 3 m/s, while the barrel is swinging upwards with a constant angular velocity of 2 rad/s. The magnitude of the absolute velocity of the shell is



- (a) 3 m/s (b) 4 m/s
(c) 5 m/s (d) 7 m/s

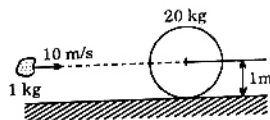
41. An elevator (lift) consists of the elevator cage and a counter weight, of mass m each. The cage and the counterweight are connected by a chain that passes over a pulley. The pulley is coupled to a motor. It is desired that the elevator should have a maximum stopping time of t seconds from a peak speed v . If the inertias of the pulley and the chain are neglected, the minimum power that the motor must have is

- (a) $\frac{1}{2}mv^2$
(b) $\frac{mv^2}{2t}$
(c) $\frac{mv^2}{t}$
(d) $\frac{2mv^2}{t}$



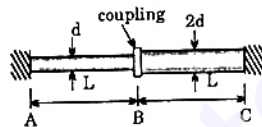
42. A 1 kg mass of clay, moving with a velocity of 10 m/s, strikes a stationary wheel and sticks to it. The solid wheel has a mass of 20 kg and a radius of 1m. Assuming that the wheel and the ground are both rigid and that the wheel is set into pure rolling motion, the angular velocity of the wheel immediately after the impact is approximately

- (a) zero
(b) $\frac{1}{3}$ rad/s
(c) $\sqrt{\frac{10}{3}}$ rad/s
(d) $\frac{10}{3}$ rad/s



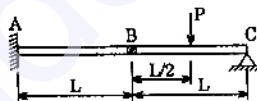
43. The two shafts AB and BC, of equal length and diameters d and $2d$, are made of the same material. They are joined at B through a shaft coupling, while the ends A and C are built-in (cantilevered). A twisting moment T is applied to the coupling. If T_A and T_C represent the twisting moments at the ends A and C, respectively, then

- (a) $T_C = T_A$
(b) $T_C = 8T_A$
(c) $T_C = 16T_A$
(d) $T_A = 16T_C$

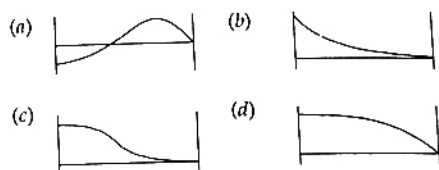
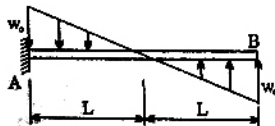


44. A beam is made up of two identical bars AB and BC, by hinging them together at B. The end A is built-in (cantilevered) and the end C is simply-supported. With the load P acting as shown, the bending moment at A is

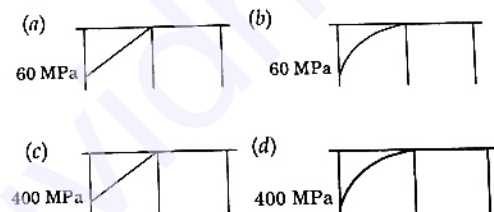
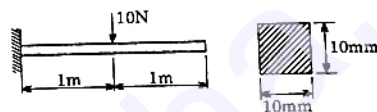
- (a) zero
(b) $\frac{PL}{2}$
(c) $\frac{3PL}{2}$
(d) indeterminate



45. A cantilever beam carries the anti-symmetric load shown, where w_0 is the peak intensity of the distributed load. Qualitatively, the correct bending moment diagram for this beam is



46. A cantilever beam has the square cross section 10 mm \times 10 mm. It carries a transverse load of 10 N. Considering only the bottom fibres of the beam, the correct representation of the longitudinal variation of the bending stress is



47. In a cam-follower mechanism, the follower needs to rise through 20 mm during 60° of cam rotation, the first 30° with a constant acceleration and then with a deceleration of the same magnitude. The initial and final speeds of the follower are zero. The cam rotates at a uniform speed of 300 rpm. The maximum speed of the follower is

- (a) 0.60 m/s
(b) 1.20 m/s
(c) 1.68 m/s
(d) 2.40 m/s

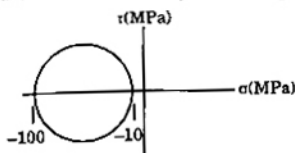
48. A rotating disc of 1 m diameter has two eccentric masses of 0.5 kg each at radii of 50 mm and 60 mm at angular positions of 0° and 150° , respectively. A balancing mass of 0.1 kg is to be used to balance the rotor. What is the radial position of the balancing mass?

- (a) 50 mm
(b) 120 mm
(c) 150 mm
(d) 280 mm

49. In a spring-mass system, the mass is 0.1 kg and the stiffness of the spring is 1 kN/m. By introducing a damper, the frequency of oscillation is found to be 90% of the original value. What is the damping coefficient of the damper?

- (a) 1.2 N.s/m
(b) 3.4 N.s/m
(c) 8.7 N.s/m
(d) 12.0 N.s/m

50. The Mohr's circle of plane stress for a point in a body is shown. The design is to be done on the basis of the maximum shear stress theory for yielding. Then, yielding will just begin if the designer chooses a ductile material whose yield strength is

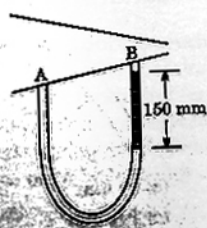


- (a) 45 MPa (b) 50 MPa
(c) 90 MPa (d) 100 MPa
51. A weighing machine consists of a 2 kg pan resting on spring. In this condition, with the pan resting on the spring, the length of the spring is 200 mm. When a mass of 20 kg is placed on the pan, the length of the spring becomes 100 mm. For the spring, the undeformed length l_0 and the spring constant k (stiffness) are
- (a) $l_0 = 220$ mm, $k = 1862$ N/m
(b) $l_0 = 210$ mm, $k = 1960$ N/m
(c) $l_0 = 200$ mm, $k = 1960$ N/m
(d) $l_0 = 200$ mm, $k = 2156$ N/m

52. A venturimeter of 20 mm throat diameter is used to measure the velocity of water in a horizontal pipe of 40 mm diameter. If the pressure difference between the pipe and throat sections is found to be 30 kPa then, neglecting frictional losses, the flow velocity is
- (a) 0.2 m/s (b) 1.0 m/s
(c) 1.4 m/s (d) 2.0 m/s

53. A U-tube manometer with a small quantity of mercury is used to measure the static pressure difference between two locations A and B in a conical section through which an incompressible fluid flows. At a particular flow rate, the mercury column appears as shown in the figure. The density of mercury is 13600 kg/m^3 and $g = 9.81 \text{ m/s}^2$. Which of the following is correct?

- (a) Flow direction is A to B and $p_A = p_B = 20 \text{ kPa}$
(b) Flow direction is B to A and $p_A = p_B = 1.4 \text{ kPa}$
(c) Flow direction is A to B and $p_B = p_A = 20 \text{ kPa}$
(d) Flow direction is B to A and $p_B = p_A = 1.4 \text{ kPa}$



54. A reversible thermodynamic cycle containing only three processes and producing work is to be constructed. The constraints are
- there must be one isothermal process,
 - there must be one isentropic process,
 - the maximum and minimum cycle pressures and the clearance volume are fixed, and
 - polytropic processes are not allowed. Then the number of possible cycles are

- (a) 1 (b) 2
(c) 3 (d) 4

55. Nitrogen at an initial state of 10 bar, 1 m^3 and 300 K is expanded isothermally to a final volume of 2 m^3 .

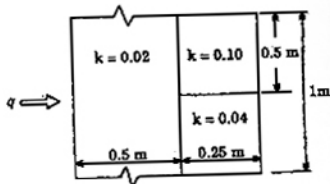
The p - v - T relation is $\left(p + \frac{a}{v^2}\right)v = RT$, where

$a > 0$. The final pressure

- (a) will be slightly less than 5 bar
(b) will be slightly more than 5 bar
(c) will be exactly 5 bar
(d) cannot be ascertained in the absence of the value of a .

56. Heat flows through a composite slab, as shown below. The depth of the slab is 1 m. The k values are in W/m.K . the overall thermal resistance in K/W is

- (a) 17.2
(b) 21.9
(c) 28.6
(d) 39.2



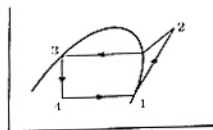
57. A small copper ball of 5 mm diameter at 500 K is dropped into an oil bath whose temperature is 300 K. The thermal conductivity of copper is 400 W/m.K , its density 9000 kg/m^3 and its specific heat 385 J/kg.K . If the heat transfer coefficient is $250 \text{ W/m}^2\text{K}$ and lumped analysis is assumed to be valid, the rate of fall of the temperature of the ball at the beginning of cooling will be, in K/s ,

- (a) 8.7 (b) 13.9
(c) 17.3 (d) 27.7

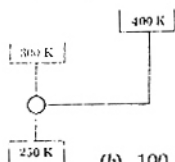
58. A solid cylinder (surface 2) is located at the centre of a hollow sphere (surface 1). The diameter of the sphere is 1 m, while the cylinder has a diameter and length of 0.5 m each. The radiation configuration factor F_{11} is

- (a) 0.375 (b) 0.625
(c) 0.75 (d) 1

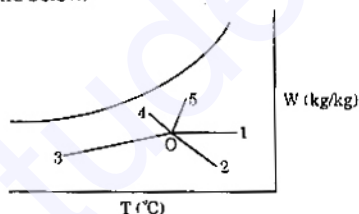
59. Hot oil is cooled from 80 to 50°C in an oil cooler which uses air as the coolant. The air temperature rises from 30 to 40°C. The designer uses a LMTD value of 26°C. The type of heat exchanger is
 (a) parallel flow (b) double pipe
 (c) counter flow (d) cross flow
60. The vapour compression refrigeration cycle is represented as shown in the figure below, with state 1 being the exit of the evaporator. The coordinate system used in this figure is



- (a) $p-h$ (b) $T-s$
 (c) $p-s$ (d) $T-h$
61. A vapour absorption refrigeration system is a heat pump with three thermal reservoirs as shown in the figure. A refrigeration effect of 100 W is required at 250 K when the heat source available is at 400 K. Heat rejection occurs at 300 K. The minimum value of heat required (in W) is



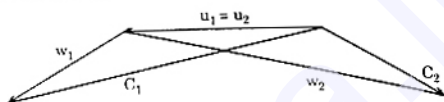
- (a) 167 (b) 100
 (c) 80 (d) 20
62. Various psychrometric processes are shown in the figure below.



Process in Figure	Name of the process
P-0-1	1. Chemical dehumidification
Q-0-2	2. Sensible heating
R-0-3	3. Cooling and dehumidification
S-0-4	4. Humidification with steam injection
T-0-5	5. Humidification with water injection

The matching pairs are
 (a) P-1, Q-2, R-3, S-4, T-5
 (b) P-2, Q-1, R-3, S-5, T-4
 (c) P-2, Q-1, R-3, S-4, T-5
 (d) P-3, Q-4, R-5, S-1, T-2

63. In the velocity diagram shown below, u = blade velocity, C = absolute fluid velocity and w = relative velocity of fluid and the subscripts 1 and 2 refer to inlet and outlet.

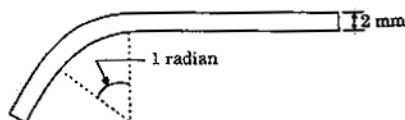


- (a) an impulse turbine
 (b) a reaction turbine
 (c) a centrifugal compressor
 (d) an axial flow compressor
64. A leaf is caught in a whirlpool. At a given instant, the leaf is at a distance of 120 m from the centre of the whirlpool. The whirlpool can be described by the following velocity distribution;

$$V_r = -\left(\frac{60 \times 10^3}{2\pi r}\right) \text{ m/s and } V_\theta = \frac{300 \times 10^3}{2\pi r} \text{ m/s,}$$

where r (in metres) is the distance from the centre of the whirlpool. What will be the distance of the leaf from the centre when it has moved through half a revolution?

- (a) 48 m (b) 64 m
 (c) 120 m (d) 142 m
65. A mould has a downsprue whose length is 20 cm and the cross sectional area at the base of the downsprue is 1 cm². The downsprue feeds a horizontal runner leading into the mould cavity of volume 1000 cm³. The time required to fill the mould cavity will be
 (a) 4.05 s (b) 5.05 s
 (c) 6.05 s (d) 7.25 s
66. A 2 mm thick metal sheet is to be bent at an angle of one radian with a bend radius of 100 mm. If the stretch factor is 0.5, the bend allowance is



- (a) 99 mm (b) 100 mm
 (c) 101 mm (d) 102 mm

67. Spot welding of two 1 mm thick sheets of steel (density = 8000 kg/m³) is carried out successfully by passing a certain amount of current for 0.1 second through the electrodes. The resultant weld nugget formed is 5 mm in diameter and 1.5 mm thick. If the latent heat of fusion of steel is 1400 kJ/kg and the effective resistance in the welding operation is 200 Ω , the current passing through the electrodes is approximately

(a) 1480 A (b) 3300 A
(c) 4060 A (d) 9400 A

68. A 600 mm \times 30 mm flat surface of a plate is to be finish machined on a shaper. The plate has been fixed with the 600 mm side along the tool travel direction. If the tool over-travel at each end of the plate is 20 mm, average cutting speed is 8m/min, feed rate is 0.3 mm/stroke and the ratio of return time to cutting time of the tool is 1:2, the time required for machining will be

(a) 8 minutes (b) 12 minutes
(c) 16 minutes (d) 20 minutes

69. The tool of an NC machine has to move along a circular arc from (5,5) to (10,10) while performing an operation. The centre of the arc is at (10,5). Which one of the following NC tool path commands performs the above mentioned operation?

(a) N010 G02 X10 Y10 X5 Y5 R5
(b) N010 G03 X10 Y10 X5 Y5 R5
(c) N010 G01 X5 Y5 X10 Y10 R5
(d) N010 G02 X5 Y5 X10 Y10 R5

70. A component can be produced by any of the four processes I, II, III and IV. Process I has a fixed cost of Rs. 20 and variable cost of Rs. 3 per piece. Process II has a fixed cost Rs. 50 and variable cost of Re. 1 per piece. Process III has a fixed cost of Rs. 40 and variable cost of Rs. 2 per piece. Process IV has a fixed cost of Rs. 10 and variable cost of Rs. 4 per piece. If the company wishes to produce 100 pieces of the component, from economic point of view it should choose

(a) Process I (b) Process II
(c) Process III (d) Process IV

71. A welding operation is time-studied during which an operator was pace-rated as 120%. The operator took, on an average, 8 minutes for producing the weld-joint. If a total of 10% allowances are allowed for this operation, the expected standard production rate of the weld-joint (in units per 8 hour day) is

(a) 45 (b) 50
(c) 55 (d) 60

72. The distribution of lead time demand for an item is as follows:

Lead time demand	Probability
80	0.20
100	0.25
120	0.30
140	0.25

The reorder level is 1.25 times the expected value of the lead time demand. The service level is

(a) 25% (b) 50%
(c) 75% (d) 100%

73. A project has six activities (A to F) with respective activity durations 7,5,6,6,8,4 days. The network has three paths A-B, C-D and E-F. All the activities can be crashed with the same crash cost per day. The number of activities that need to be crashed to reduce the project duration by 1 day is

(a) 1 (b) 2
(c) 3 (d) 6

74. A company has two factories S1, S2 and two warehouses D1, D2. The supplies from S1 and S2 are 50 and 40 units respectively. Warehouse D1 requires a minimum of 20 units and a maximum of 40 units. Warehouse D2 requires a minimum of 20 units and, over and above, it can take as much as can be supplied. A balanced transportation problem is to be formulated for the above situation. The number of supply points, the number of demand points, and the total supply (or total demand) in the balanced transportation problem respectively are

(a) 2, 4, 90 (b) 2, 4, 110
(c) 3, 4, 90 (d) 3, 4, 110

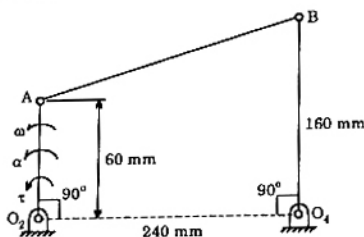
75. Two tools P and Q have signatures 5°5'6" 6°8'30" 0° and 5°5'7" 7°8'15" 0° (both ASA) respectively. They are used to turn components under the same machining conditions. If h_p and h_Q denote the peak-to-valley heights of surfaces produced by the tools P and Q, the ratio h_p/h_Q will be

(a) $\frac{\tan 8^\circ + \cot 15^\circ}{\tan 8^\circ + \cot 30^\circ}$ (b) $\frac{\tan 15^\circ + \cot 8^\circ}{\tan 30^\circ + \cot 8^\circ}$
(c) $\frac{\tan 15^\circ + \cot 7^\circ}{\tan 30^\circ + \cot 7^\circ}$ (d) $\frac{\tan 7^\circ + \cot 15^\circ}{\tan 7^\circ + \cot 30^\circ}$

Common Data Questions

Common Data for Questions 76, 77, 78:

An instantaneous configuration of a four-bar mechanism, whose plane is horizontal, is shown in the figure below. At this instant, the angular velocity and angular acceleration of link O_2A are $\omega = 8 \text{ rad/s}$ and $\alpha = 0$, respectively, and the driving torque (τ) is zero. The link O_2A is balanced so that its centre of mass falls at O_2 .



76. Which kind of 4-bar mechanism is O_2ABO_4 ?
 (a) Double-crank mechanism
 (b) Crank-rocker mechanism
 (c) Double-rocker mechanism
 (d) Parallelogram mechanism
77. At the instant considered, what is the magnitude of the angular velocity of Q_4B ?
 (a) 1 rad/s
 (b) 3 rad/s
 (c) 8 rad/s
 (d) $\frac{64}{3} \text{ rad/s}$
78. At the same instant, if the component of the force at joint A along AB is 30 N, then the magnitude of the joint reaction at O_2
 (a) is zero
 (b) is 30 N
 (c) is 78 N
 (d) cannot be determined from the given data

Common Data for Questions 79, 80:

In two air standard cycles – one operating on the Otto and the other on the Brayton cycle – air is isentropically compressed from 300 to 450 K. Heat is added to raise the temperature to 600 K in the Otto cycle and to 550 K in the Brayton cycle.

79. If η_O and η_B are the efficiencies of the Otto and Brayton cycles, then
 (a) $\eta_O = 0.25$, $\eta_B = 0.18$
 (b) $\eta_O = \eta_B = 0.33$
 (c) $\eta_O = 0.5$, $\eta_B = 0.45$
 (d) it is not possible to calculate the efficiencies unless the temperature after the expansion is given

80. If W_O and W_B are work outputs per unit mass, then
 (a) $W_O > W_B$
 (b) $W_O < W_B$
 (c) $W_O = W_B$
 (d) it is not possible to calculate the work outputs unless the temperature after expansion is given

Linked Answer Questions: Q.81a to Q.85b carry two marks each.

Statement for Linked Answer Questions 81a and 81b:

The complete solution of the ordinary differential

$$\text{equation } \frac{d^2 y}{dx^2} + p \frac{dy}{dx} + qy = 0 \text{ is } y = c_1 e^{-x} + c_2 e^{-3x}$$

81a. Then, p and q are

- (a) $p = 3$, $q = 3$
 (b) $p = 3$, $q = 4$
 (c) $p = 4$, $q = 3$
 (d) $p = 4$, $q = 4$

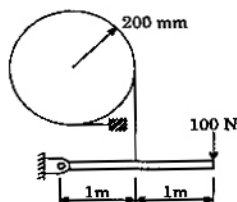
81b. Which of the following is a solution of the

$$\text{differential equation } \frac{d^2 y}{dx^2} + p \frac{dy}{dx} + (q+1)y = 0 ?$$

- (a) e^{-3x}
 (b) xe^{-x}
 (c) xe^{-2x}
 (d) $x^2 e^{-2x}$

Statement for Linked Answer Questions 82a and 82b

A band brake consists of a lever attached to one end of the band. The other end of the band is fixed to the ground. The wheel has a radius of 200 mm and the wrap angle of the band is 270° . The braking force applied to the lever is limited to 100 N, and the coefficient of friction between the band and the wheel is 0.5. No other information is given.



- 82a. The maximum tension that can be generated in the band during braking is
 (a) 1200 N
 (b) 2110 N
 (c) 3224 N
 (d) 4420 N
- 82b. The maximum wheel torque that can be completely braked is
 (a) 200 N.m
 (b) 382 N.m
 (c) 604 N.m
 (d) 844 N.m

Statement for Linked Answer Questions 83a and 83b:

Consider a linear programming problem with two variables and two constraints. The objective function is: Maximize $X_1 + X_2$. The corner points of the feasible region are (0,0), (0,2), (2,0) and (4/3, 4/3)

83a. If an additional constraint $X_1 + X_2 \leq 5$ is added, the optimal solution is

- (a) $\left(\frac{5}{3}, \frac{5}{3}\right)$ (b) $\left(\frac{4}{3}, \frac{4}{3}\right)$
(c) $\left(\frac{5}{2}, \frac{5}{2}\right)$ (d) (5, 0)

83b. Let Y_1 and Y_2 be the decision variables of the dual and v_1 and v_2 be the slack variables of the dual of the given linear programming problem. The optimum dual variables are

- (a) Y_1 and Y_2 (b) Y_1 and v_1
(c) Y_1 and v_2 (d) v_1 and v_2

Statement for Linked Answer Questions 84a and 84b:

The following table of properties was printed out for saturated liquid and saturated vapour of ammonia. The titles for only the first two columns are available. All that we know is that the other columns (columns 3 to 8) contain data on specific properties, namely, internal energy (kJ/kg), enthalpy (kJ/kg) and entropy (kJ/kg, K).

(K)	p (kPa)						
-20	190.2	88.76	0.3657	89.05	5.6155	1299.5	1418.0
0	429.6	179.69	0.7114	180.36	5.3309	1318.0	1442.2
20	857.5	272.89	1.0408	274.30	5.0860	1332.2	1460.2
40	1554.9	368.74	1.3574	371.43	4.8662	1341.0	1470.2

84a. The specific enthalpy data are in columns

- (a) 3 and 7 (b) 3 and 8
(c) 5 and 7 (d) 5 and 8

84b. When saturated liquid at 40°C is throttled to -20°C, the quality at exit will be

- (a) 0.189 (b) 0.212
(c) 0.231 (d) 0.788

Statement for Linked Answer Questions 85a and 85b:

An un-insulated air conditioning duct of rectangular cross section 1m × 0.5 m, carrying air at 20°C with a velocity of 10 m/s, is exposed to an ambient of 30°C. Neglect the effect of duct construction material. For air in the range of 20-30°C, data are as follows: thermal conductivity = 0.025 W/m.K; velocity = 18 μPa.s; Prandtl number = 0.73; density = 1.2 kg/m³. The laminar flow Nusselt number is 3.4 for constant wall temperature conditions and, for turbulent flow, $Nu = 0.023 Re^{0.8} Pr^{0.4}$

85a. The Reynolds number for the flow is

- (a) 444 (b) 890
(c) 4.44×105 (d) 5.33×105

85b. The heat transfer per metre length of the duct, in watts, is

- (a) 3.8 (b) 5.3
(c) 89 (d) 769

ANSWERS

1. (a)	2. (b)	3. (a)	4. (c)	5. (d)	6. (d)	7. (a)	8. (a)	9. (c)	10. (c)
11. (a)	12. (a)	13. (d)	14. (d)	15. (a)	16. (d)	17. (c)	18. (b)	19. (b)	20. (d)
21. (a)	22. (d)	23. (b)	24. (a)	25. (c)	26. (a)	27. (b)	28. (d)	29. (c)	30. (a)
31. (a)	32. (c)	33. (a)	34. (c)	35. (d)	36. (a)	37. (c)	38. (d)	39. (d)	40. (c)
41. (c)	42. (b)	43. (a)	44. (b)	45. (c)	46. (a)	47. (d)	48. (c)	49. (c)	50. (c)
51. (b)	52. (d)	53. (a)	54. (a)	55. (b)	56. (d)	57. (a)	58. (c)	59. (d)	60. (a)
61. (c)	62. (b)	63. (b)	64. (b)	65. (b)	66. (c)	67. (c)	68. (b)	69. (d)	70. (b)
71. (a)	72. (d)	73. (c)	74. (c)	75. (b)	76. (b)	77. (b)	78. (d)	79. (b)	80. (a)
81a. (c)	81b. (c)	82a. (b)	82b. (b)	83a. (b)	83b. (d)	84a. (d)	84b. (b)	85a. (c)	85b. (d)



EXPLANATIONS

1. A line integral and a surface integral is connected by Stokes theorem.

$$\Rightarrow v_t = 0 = 2$$

2. Probability of defective item = $\frac{10}{100} = 0.1$

$$\text{and } a = \frac{dv}{dt} = 12t + 2,$$

Probability of not defective item = $1 - 0.1 = 0.9$

$$\Rightarrow a_t = 0 = 2$$

So, probability that exactly 2 of the chosen items are defective

$$= {}^{10}C_2 (0.1)^2 (0.9)^8 = 0.1937.$$

7. Force at mean position is zero.

8. Rod is not restrained but completely free

10. Number of degree of freedom,

$$\begin{aligned} n &= 3(l-1) - 2J - h \\ &= (3 \times 7) - (2 \times 9) - 0 = 3 \end{aligned}$$

3. $I = \int_{-a}^a (\sin^6 x + \sin^7 x) dx$

12. Sommerfeld Number, also known as Bearing Characteristic Number,

$$S = \frac{Z_n}{P} \cdot \left(\frac{D}{C_d} \right)^2$$

$$= 2 \int_0^a \sin^6 x dx + 0$$

$$= 2 \int_0^a \sin^6 x dx,$$

13. $\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = 0 \dots (i)$ (Laplace Equation should be satisfied)

Make a square matrix for higher possible rank, i.e.,

$$\therefore \dots = -\frac{\partial \phi}{\partial x} \quad \text{and} \quad v = -\frac{\partial \phi}{\partial y}$$